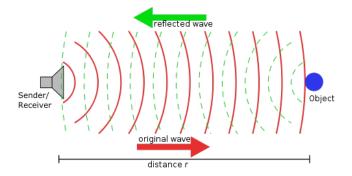
Fast Matched Filter and Group Representation: What? Why? How?

Speaker: Shamgar Gurevich, UW Madison.

Abstract: In the discrete radar problem we design a function (waveform) S(t) in the Hilbert space $\mathcal{H} = \mathbb{C}(\mathbb{Z}/p)$ of complex valued functions on $\mathbb{Z}/p = \{0, ..., p-1\}$, the integers modulo a prime number p >> 0. We transmit the function S(t) using the radar to the object that we want to detect. The wave S(t) hits the object, and is reflected back via the echo wave $E(t) \in \mathbb{C}(\mathbb{Z}/p)$, which has the form

$$E(t) = e^{\frac{2\pi i}{p}\omega_0 t} \cdot S(t+\tau_0) + N(t),$$

where N(t) is some Gaussian white noise with mean zero, and $\tau_0, \omega_0 \in \mathbb{Z}/p$ encode the distance from, and velocity of, the object.



Problem (discrete radar problem) Extract τ_0, ω_0 from *E* and *S*.

In my lecture I first introduce the classical matched filter (MF) algorithm that suggests the 'traditional' way (using fast Fourier transform) to solve the discrete radar problem in order of $p^2 \cdot \log(p)$ operations. I will then explain how to use techniques from group representation theory to design (construct) waveforms S(t) which enable us to introduce a fast matched filter (FMF) algorithm, that we call the "flag algorithm", which solve the discrete radar problem in a much faster way of order of $p \cdot \log(p)$ operations.

This is a joint work with A. Fish (Mathematics, UW Madison), R. Hadani (Mathematics, UT Austin), A. Sayeed (Electrical Engineering, UW Madison), and O. Schwartz (Computer Science, UC Berkeley).

I will assume knowledge of elementary linear algebra.